

The set of all values of λ for which the system of linear equations :

$$\left. \begin{aligned} 2x_1 - 2x_2 + x_3 &= \lambda x_1 \\ 2x_1 - 3x_2 + 2x_3 &= \lambda x_2 \\ -x_1 + 2x_2 &= \lambda x_3 \end{aligned} \right\}$$

$$\Rightarrow (2 - \lambda)x_1 - 2x_2 + x_3 = 0$$

$$2x_1 - (3 + \lambda)x_2 + 2x_3 = 0$$

$$-x_1 + 2x_2 - \lambda x_3 = 0$$

- has a non-trivial solution,
- (1) contains two elements.
 - (2) contains more than two elements.
 - (3) is an empty set.
 - (4) is a singleton.

Since they have non-trivial solution

$$\Delta = \begin{vmatrix} 2 - \lambda & -2 & 1 \\ 2 & -(3 + \lambda) & 2 \\ -1 & 2 & -\lambda \end{vmatrix} = 0$$

$$\Rightarrow \lambda^3 + \lambda^2 - 5\lambda + 3 = 0$$

$$\Rightarrow (\lambda - 1)^2 (\lambda + 3) = 0$$

$$\Rightarrow \lambda = 1, 3 \Rightarrow \text{Two elements}$$

\therefore Correct option is (1)